ing force constants from $a b$ initio calculations on 1a and bending force constants obtained by interpolation of pertinent empirical data. These force constants (seven in all) lead to calculated frequencies ${ }^{23}$ for 1a ( $\nu_{2}=1236 \mathrm{~cm}^{-1}, \nu_{3}=661 \mathrm{~cm}^{-1}$, and $\nu_{4}=576 \mathrm{~cm}^{-1}$ ) and the monodeuterio derivative (vide infra), in excellent agreement with the observed bands. We also note that the SCF ab initio calculations lead to a predicted square equilibrium geometry $\left(R_{\mathrm{e}}=1.434 \AA\right)$ for the triplet state $\left({ }^{3} \mathrm{~A}_{2 g}\right)$ of $1 a^{26}$ similar to Dewar's semiempirical result. ${ }^{27}$ Furthermore, calculations using the general valence bond method (GVB) ${ }^{31}$ indicate that the singlet lies $7.7 \mathrm{kcal} / \mathrm{mol}$ above the triplet at the triplet equilibrium geometry ( $D_{4 n}$ ) and is unstable to a rectangular distortion.

The above discussion has focused on the likelihood of a square geometry for 1 a ; we emphasize that any appreciable rectangular distortion of the square would be expected to cause significant splitting of the degenerate $1236-\mathrm{cm}^{-1}$ mode ( $\nu_{2}$ ). A mild rectangular distortion ( $R_{\mathrm{CC}}$ and $R_{\mathrm{CC}}=1.37$ and $1.46 \AA$, respectively) leads to a predicted splitting of $100 \mathrm{~cm}^{-1}$, if the above force constants are employed, with $f_{\mathrm{RR}}$ being allowed to vary with bond length according to Badger's rule. ${ }^{32}$ Correspondingly larger splitting would be likely for more pronounced distortions (e.g., the equilibrium singlet geometry of 1 a for which we calculate $\mathrm{C}-\mathrm{C}$ bond distances of 1.34 and $1.56 \AA$ using the GVB ${ }^{31}$ method).

The above assignments receive strong confirmation from the spectrum of monodeuteriocyclobutadiene (1b) obtained by photolyzing bicyclo[2.2.0]pyran-2-one- $6-d(2 \mathrm{~b})^{12 \mathrm{~b}, \mathrm{c}}$ in the manner described for 2 a previously. Not surprisingly, the allowed modes of the parent 1a also show up as strong bands, appropriately shifted and split in the spectrum (Figure 1b) of 1b, as confirmed by inspection of the location of the bands and by the theoretical calculations. The slight shift

1a and scaled by the same factor (0.877) which brings the calculated and experimental benzene force constants into agreement; the remaining interaction constant between the $\mathrm{C}-\mathrm{C}$ bonds was assumed to be zero); ${ }^{25}$ $f_{\beta \beta}=0.30 \mathrm{mdyn} \AA / \mathrm{rad}^{2}$ (estimated from standard values ${ }^{28}$ on the basis of calculated ${ }^{29} \mathrm{~s}$ character ( $\mathrm{sp}^{1.6}$ ) for the C-H bonds); $f_{\alpha \alpha}=1.30$ and $f_{\gamma \gamma}=1.30 \mathrm{mdyn} \AA / \mathrm{rad}^{2}$ (based on available data for cyclobutane ${ }^{\text {36a }}$ and benzene ${ }^{3 \mathrm{cb}}$ ); $f_{\mathrm{R} \beta}=0.36 \mathrm{mdyn} / \mathrm{rad}$ (from benzene, ${ }^{30 \mathrm{~b}}$, with signs determined by assuming hybrid orbital following); and $f_{\beta \beta^{\prime}}=-0.05$ mdyn $\AA / \mathrm{rad}^{2}$ (based on the out-of-plane benzene modes ${ }^{30 c}$ ). This unbiased selection from a priori and standard empirical values adequately reproduces the observed bands.
(23) The computer program was written by J. H. Schactschneider as described in Technical Report No. 231-64 and 57-65, Shell Development Co., Emeryville, Calif., 1964.
(24) R. Ditchfield, W. J. Hehre, and J. A. Pople, J. Chem. Phys., 54, 724 (1971).
(25) The $\mathrm{C}-\mathrm{C}$ force constants were based on the square equilibrium triplet calculation, ${ }^{26}$ since the calculated equilibrium geometry ( $D_{2 h}$ ) and force constants for the singlet were not consistent with the observed spectrum of 1a; vide infra.
(26) (a) A previous minimal basis $a b$ initio calculation (limited CI) suggested a slightly rectangular equilibrium triplet. 26 b However, the more flexible, extended basis ${ }^{24}$ used in the present calculations predicts a square geometry. (b) R. J. Buenker and S. D. Peyerimhoff, J. Chem. Phys., 48, 354 (1968).
(27) M. J. S. Dewar, M. C. Kahn, and N. Trinjastic, J. Amer. Chem. Soc., 93, 3437 (1971).
(28) Reference 14, p 193.
(29) From the localized molecular orbitals; see, e.g., M. D. Newton and J. M. Schulman, J. Amer. Chem. Soc., 94, 773 (1972).
(30) (a) T. P. Wilson, J. Chem. Phys., 11, 369 (1943); (b) J. C. Duinker and I. M. Mills, Spectrochim. Acta, Part A, 24, 417 (1968); (c) F. A. Miller and B. L. Crawford, J. Chem. Phys., 14, 282 (1946).
(31) W. J. Hunt, P. J. Hay, and W. A. Goddard, III, J. Chem. Phys., 57, 738 (1972). We thank the authors for providing us with a version of their program.
(32) H. S. Johnston, "Gas Phase Reaction Rate Theory," Ronald Press, New York, N. Y., 1966.
in the frequency of the band at $1236 \mathrm{~cm}^{-1}$ in 1a to $1224 \mathrm{~cm}^{-1}$ upon isotopic substitution confirms that it is predominantly a distortion of the carbon framework $\left(\nu_{2}\right)$.

Assuming that bands at 653,594 , and $540 \mathrm{~cm}^{-1}$ arise from the $\nu_{3}$ and $\nu_{4}$ modes of the parent 1a, their location is only consistent (in the harmonic approximation) with the assignment of the band at $540 \mathrm{~cm}^{-1}$ to $\nu_{4}$, and the bands at 653 and $594 \mathrm{~cm}^{-1}$ to the two split components ( $\nu_{3 \mathrm{~s}}$ and $\nu_{3 \mathrm{~b}}$ ) of the degenerate parent mode $\left(\nu_{3}\right) .{ }^{33}$ The calculations described above are in good agreement with this analysis, predicting only a small splitting of the $1236-\mathrm{cm}^{-1}$ band. (Similar calculations for the $1,2-$ and 1,3 -dideuterio derivatives give splittings of 17 and $32 \mathrm{~cm}^{-1}$, respectively.) A much larger splitting is predicted for the in-plane bending mode ( $\nu_{3}$ ), with the unshifted line (in which the C-D bend does not participate) assigned to the $\mathrm{A}_{1}$ component (calcd value, $661 \mathrm{~cm}^{-1}$ ), and the $594-\mathrm{cm}^{-1}$ band assigned to the $B_{1}$ component (calcd, $616 \mathrm{~cm}^{-1}$ ). The calculations yield a value of $527 \mathrm{~cm}^{-1}$ for the remaining parent mode $\left(\nu_{4}\right)$, thus completing the confirmation of the above assignment. In addition to the aforementioned intense bands in Figure 1b, arising from the active parent modes, we also note an intense band at $460 \mathrm{~cm}^{-1}$ which, from our calculations ( $477 \mathrm{~cm}^{-1}$ ), is indicated to be almost a pure CH bending mode of $B_{1}$ symmetry. The appearance of spectra 1 a and $\mathbf{1 b}$, combined with theoretical predictions of the splittings of $\mathrm{E}_{\mathrm{u}}$ modes upon descent into $C_{20}$ symmetry, solidly support assignment of the $1236-$ and $653-\mathrm{cm}^{-1}$ bands to degenerate modes of square cyclobutadiene.

Although the present results are consistent with a square equilibrium geometry, there remains the possibility of an effective square geometry arising, perhaps, from rapid equilibration between slightly distorted squares separated by small barriers. The present $a b$ initio calculations rule out such a possibility for any distortion of the triplet; since the equilibrium singlet corresponds to a strongly distorted square (a rectangle with normal single and double bond lengths), the larger barrier separating the two rectangular forms should prohibit rapid equilibration between them.

Acknowledgment. The award of a Frederick Gardner Cottrell Grant from the Research Corporation to A. Krantz is gratefully acknowledged This work was performed in part under the auspices of the U.S. Atomic Energy Commission (M. D. N.).
(33) E. B. Wilson, Jr., J. C. Decius, and P. C. Cross, "Molecular Vibrations," McGraw-Hill, New York, N. Y., 1955, p 190.

## A. Krantz,* C. Y. Lin

Department of Chemistry, State University of New York Stony Brook, New York 11790
M. D. Newton*

Department of Chemistry, Brookhaven National Laboratory
Upton, New York 11973
Received December 7, 1972

## Prostaglandin Synthesis. I. An Improved Synthesis through Bicyclo[3.1.0]hexane Intermediates

Sir:
The potent pharmacological properties of the various members of the prostaglandin family and their limited supply from natural sources have prompted intensive
efforts directed at their synthesis. ${ }^{1-4}$ In several cases these have resulted in elegant, highly stereocontrolled syntheses. ${ }^{5-10}$
This report details a new, efficient synthesis of prostaglandins. Norbornadiene was oxidized as described by Meinwald, et al., ${ }^{11}$ to the bicyclic aldehyde 1. Treatment of crude 1 with neopentyl glycol and a trace of mild acid in methylene chloride at $25^{\circ}$ afforded the crystalline acetal $2, \mathrm{mp} 55-55.5^{\circ}$ (61\% from norbornadiene). ${ }^{12}$ Reaction of 2 with dichloroketene led to the dichlorocyclobutanone 3, mp 97-99 ${ }^{\circ}(81 \%),{ }^{13-16}$ which on reduction with zinc and ammonium chloride in methanol gave a nearly quantitative yield of cyclobutanone 4 [ir $\left.\left(\mathrm{CH}_{2} \mathrm{Cl}_{2}\right) 1770 \mathrm{~cm}^{-1}(\mathrm{C}=\mathrm{O})\right] .{ }^{17}$


$$
\begin{array}{ll}
1, \mathrm{R}=\mathrm{CHO} & \left.3, \mathrm{X}=\mathrm{Cl} ; \mathrm{R}=\mathrm{CH}\left(\mathrm{OCH}_{2}\right)_{2} \mathrm{C}_{2} \mathrm{CH}_{3}\right)_{2} \\
2, \mathrm{R}=\mathrm{CH}\left(\mathrm{OCH}_{2}\right)_{2} \mathrm{C}\left(\mathrm{CH}_{3}\right)_{2} & \left.4, \mathrm{X}=\mathrm{H} ; \mathrm{R}=\mathrm{CH}\left(\mathrm{OCH}_{2}\right)_{2} \mathrm{CCH}_{3}\right)_{2}
\end{array}
$$

The crude 4 was resolved in the following manner. Treatment of 4 with $l$-ephedrine and a trace of $p$ toluenesulfonic acid in refluxing benzene for 24 hr produced diastereomeric oxazolidines which were purified by crystallization from methanol, mp 159-166 ${ }^{\circ}$ (70\% of theory for a resolution from 3). Hydrolysis with THF-water-HOAc (5:5:1) at $25^{\circ}$ afforded the resolved ketone 4, mp 43-47 ${ }^{\circ}$. ${ }^{18}$

Oxidation of 4 with $m$-chloroperbenzoic acid produced the lactone acetal 5, mp 129-131 ${ }^{\circ}, \alpha \mathrm{D}+9^{\circ}$ (c $0.9, \mathrm{MeOH})(90 \%$ from oxazolidine). Hydrolysis of 5 with $88 \%$ formic acid gave a $95 \%$ yield of the lactone aldehyde 6, $\mathrm{mp} 61-64^{\circ}, \alpha \mathrm{D}-30^{\circ}(c 0.5, \mathrm{MeOH}$ ).

Wittig condensation of aldehyde 6 with $n$-hexyltriphenylphosphonium bromide afforded olefin 7 [nmr $\left(\mathrm{CDCl}_{3}\right) \delta 5.7(\mathrm{~d}$ of $\left.\mathrm{t}, 1, J=7,11 \mathrm{~Hz})\right]$ in $93 \%$ yield.
(1) E. W. Horton, "Prostaglandins, Monographs on Endocrinology," Vol. 7, Springer-Verlag, New York, N. Y., 1971.
(2) S. M. M. Karim, Ed., "The Prostaglandins," Medicinal and Technical Publishing Co., Ltd., Oxford, 1972.
(3) P. Ramwell and J. E. Shaw, Ed., Ann. N. Y. Acad. Sci., 180 (1971).
(4) J. E. Pike, Fortsíhr. Chem. Org. Naturst., 28, 313 (1971).
(5) U. F. Axen, J. L. Thompson, and J. E. Pike, Chem. Commun., 602 (1970), and references therein.
(6) E. J. Corey, S. M. Albonico, U. Koelliker, T. K. Schaaf, and R. K. Varma, J. Amer. Chem. Soc., 93, 1491 (1971), and references therein.
(7) J. Fried, J. C. Sih, C. H. Lin, and P. Dalven, J. Amer. Chem. Soc., 94, 4342, 4343 (1972), and references therein.
(8) C. J. Sih, R. G. Salomon, P. Price, G. Perruzzotti, and R. Sood, Chem. Commun., 240 (1970); C. J. Sih, et al., J. Amer. Chem. Soc., 94, 3643 (1972).
(9) D. Taub, R. D. Hoffsommer, C. H. Kuo, H. L. Slates, Z. S. Zelawski, and N. L. Wendler, Chem. Commun., 1258 (1970).
(10) F. S. Alverez, D. Wren, and A. Prince, J. Amer. Chem. Soc., 94, 7823 (1972); A. F. Kluge, K. G. Untch, and J. H. Fried, ibid., 94, 7827 (1972).
(11) (a) J. Meinwald, S. S. Labana, and M. S. Chadha, J. Amer. Chem. Soc., 85, 582 (1963); (b) J. Meinwald, S. S. Labana, and G. H. Wahl, Jr., Tetrahedron Lett., 1789 (1965).
(12) These conditions for the conversion of norbornadiene to 2 were developed by Dr. J. E. Huber of The Upjohn Co.
(13) H. C. Stevens, D. A. Reich, D. R. Brandt, K. R. Fountain, and E. J. Gaughan, J. Amer. Chem. Soc., 87, 5257 (1965).
(14) L. Ghosez, R. Montaigne, and P. Mollet, Tetrahedron Lett., 135(1966).
(15) M. Rey, U. A. Huber, and A. S. Dreiding, ibid., 3583 (1968).
(16) E. J. Corey, Z. Arnold, and J. Hutton, ibid., 307 (1970).
(17) The noncrystalline products were characterized by ir and nmr spectra.
(18) For further details on the resolution see R. C. Kelly and V. VanR heenen, Tetrahedron Lett., in press.


$\begin{aligned} 5, \mathrm{R} & =\mathrm{CH}\left(\mathrm{OCH}_{2}\right)_{2} \mathrm{C}\left(\mathrm{CH}_{3}\right)_{2} \\ 6, \mathrm{R} & =\mathrm{CHO}\end{aligned}$

$$
6, \mathrm{R}=\mathrm{CHO}
$$

A number of routes from 7 to diols 10 and 11 were investigated. It was found that the best overall yield was obtained by modification of a previously described method. ${ }^{19-21}$ Thus, oxidation of 7 with $m$-chloroperbenzoic acid in methylene chloride containing suspended potassium bicarbonate gave epoxide 8 in nearly quantitative yield. Hydrolysis of 8 in acetone-waterformic acid (65:33:2) produced a mixture containing $\mathbf{7 5 \%}$ of the glycols 9 and $25 \%$ of the diols 10 and 11 .


9

$10, \mathrm{R}_{1}=\mathrm{H} ; \mathrm{R}_{2}=\mathrm{OH}$
$11, \mathrm{R}_{1}=\mathrm{OH} ; \mathrm{R}_{2}=\mathrm{H}$
Treatment of this mixture with dry formic acid ${ }^{22,23}$ at room temperature for $2-3 \mathrm{hr}$ followed by treatment with potassium carbonate and methanol led to a new mixture of glycols and diols.

The desired $15 \alpha$-diol 10 could be isolated chromatographically from this mixture in $25 \%$ yield. The remaining material containing $15 \beta$-diol 11 and starting glycols 9 could be reintroduced into dry formic acid for recycle. After two recycles an overall yield of $45 \%$ of $15 \alpha$-diol was obtained from epoxide 7.

The diol 10 prepared as herein described is identical with that obtained by Corey and coworkers ${ }^{24}$ and has been converted to $\mathrm{PGF}_{2 \alpha}$ and $\mathrm{PGE}_{2}$ identical with the natural materials.

Thus, an efficient synthesis of $\mathrm{PGF}_{2 \alpha}$ and $\mathrm{PGE}_{2}$ through bicyclo[3.1.0]hexane intermediates has been achieved. The most complex step in this synthesis, the opening of the cyclopropylcarbinyl system, is still under investigation and may be the subject of a later publication.

Acknowledgments. We are grateful to Dr. H. A. Karnes of The Upjohn Co. for large-scale preparations and an authentic sample of lactone diol $\mathbf{1 0}$ and to The Upjohn Physical and Analytical Department for ir and nmr spectral data.
(19) G. Just and Ch. Simonovitch, Tetrahedron Lett., 2093 (1967).
(20) K. G. Holden, B. Hwang, K. R. Williams, J. Weinstock, M. Harman, and J. A. Weisbach, Tetrahedron Lett., 1569 (1968).
(21) G. Just, Ch. Simonovitch, F. H. Lincoln, W. P. Schneider, U. Axen, G. B. Spero, and J. E. Pike, J. Amer. Chem. Soc., 91,5364 (1969). (22) S. Winstein and H. Marshall, J. Amer. Chem. Soc., 74, 1120 (1952).
(23) It was necessary that the formic acid be as dry as possible for best results. The much lower yields obtained with similar compounds by earlier workers ${ }^{19-21}$ may be a result of using wet formic acid.
(24) E. J. Corey, T. K. Schaaf, W. Huber, U. Koelliker, and N. M. Weinshenker, J. Amer. Chem. Soc., 92, 397 (1970).

Robert C. Kelly,* Verlan VanRheenen I. Schletter, M. D. Pillai The Upjohn Company Kalamazoo, Michigan 49001 Received December 5, 1972

